

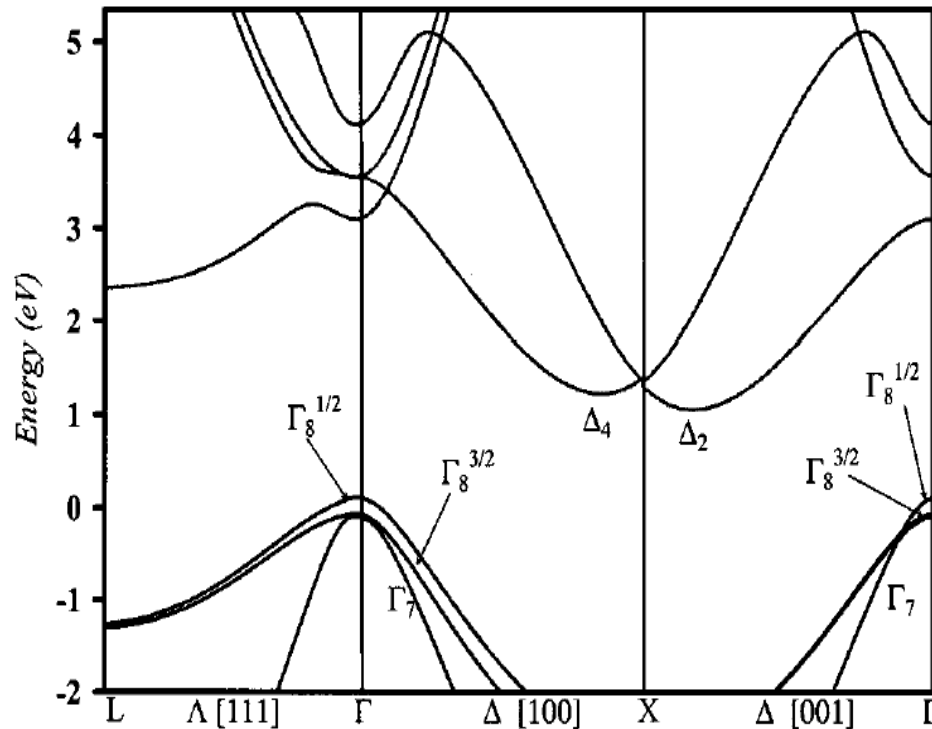
Quantum Well Model for

Strained MOSFET

Contents

- **Strained silicon quantum well model**
- **Biaxial tensile strained Si/SiGe MOSFET (theory and experiment)**
- **Uniaxial strained MOSFET (simulation)**
- **Summary**

Strained Silicon



Strained Si on SiGe (Richard et. Al. J. Appl. Phys. Vol. 94,1795)

Complete first principle band Structure model too difficult To be included in 3D drift-Diffusion solver. Use Composition parameterization Instead.

Material macro needs for all composition range:

- Strained bandgap for differen valleys.**
- DOS masses for each valley, for both perpendicular and parallel directions.**
- Bandgap discontinuities.**
- Physical based anisotropic mobility.**

Crosslight's Strained Silicon Mobility Model

Crosslight's semi-classical valley-averaged mobility model.

- 1) **MOS mobility change = valley dependent bulk mobility averaged over valley subbands in quantized states in MOS conduction channel.**
- 2) **Valley dependent bulk mobility change = effective mass change (acoustic-phonon intravalley scattering part) + scattering suppression due to band valley splitting (optical phonon part).**

Bulk Silicon Mobility

Intra-valley Acoustic Phonon Scattering part:

$$\mu_{ac} = \frac{2^{3/2} \sqrt{\pi} e \hbar^4 \rho v_s^2}{3 m^{*5/2} D_{ac}^2 (k_B T)^{3/2}} \propto T^{-1.5}$$

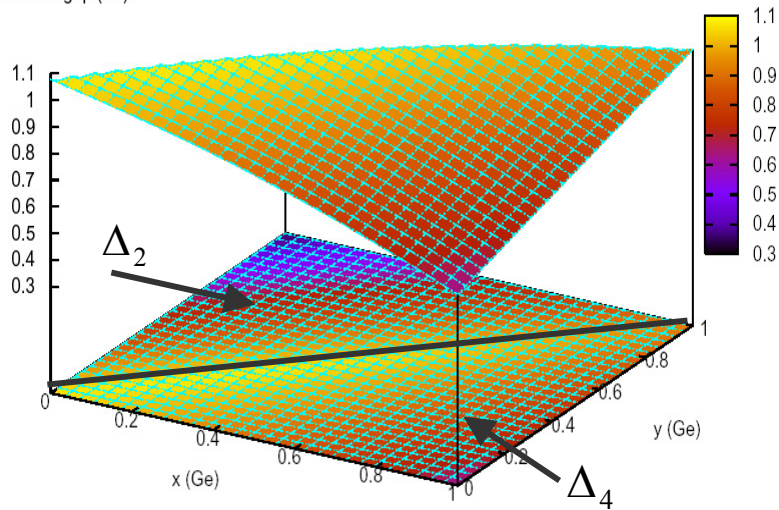
Ref: K. Uchida and J. Koga, "Mobility in Si MOSFETs",
short course at Symposium on Nano Devices
Technology **SNDT**, (Hsinchu, Taiwan), May **2004**.

**Bulk valley mobility is calibrated against bulk silicon
and biaxial strained Si/SiGe system.**

Parameterization of Strained Silicon Band Structure

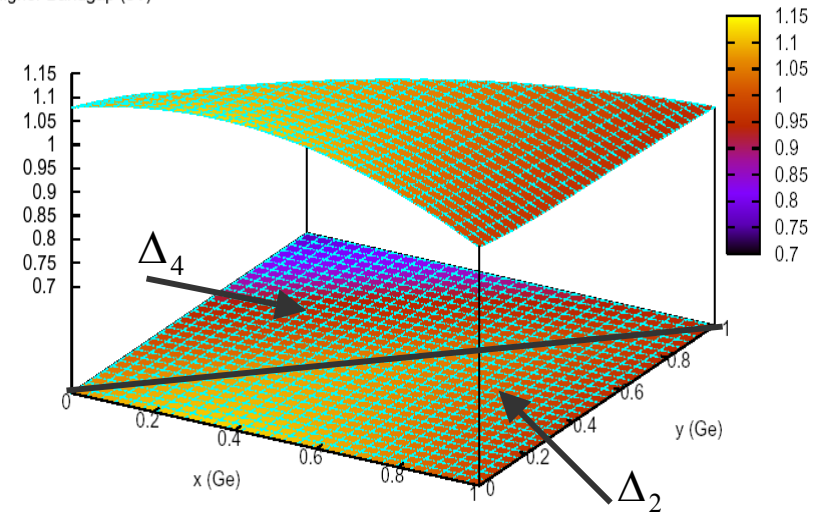
Strained Si(1-x)Ge(x)/Unstrained Si(1-y)Ge(y)

Lower Bandgap (eV)



Strained Si(1-x)Ge(x)/Unstrained Si(1-y)Ge(y)

Higher Bandgap (eV)



Implemented in Crosslight material macro library

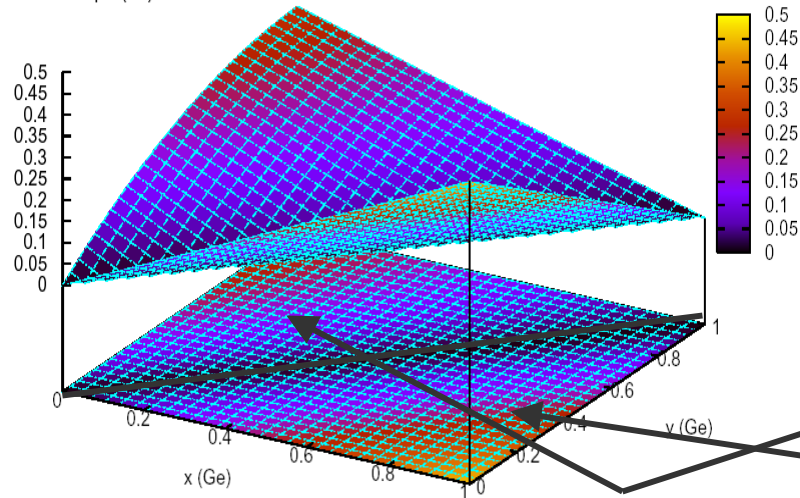
Strained Si(1-x)Ge(x) on relaxed Si(1-y)Ge(y) (Rieger&Vogl, Phys. Rev B48, 14276)

Parameterization of Valence Split & Band Discont.

Strained $\text{Si}(1-x)\text{Ge}(x)$ /Unstrained $\text{Si}(1-y)\text{Ge}(y)$

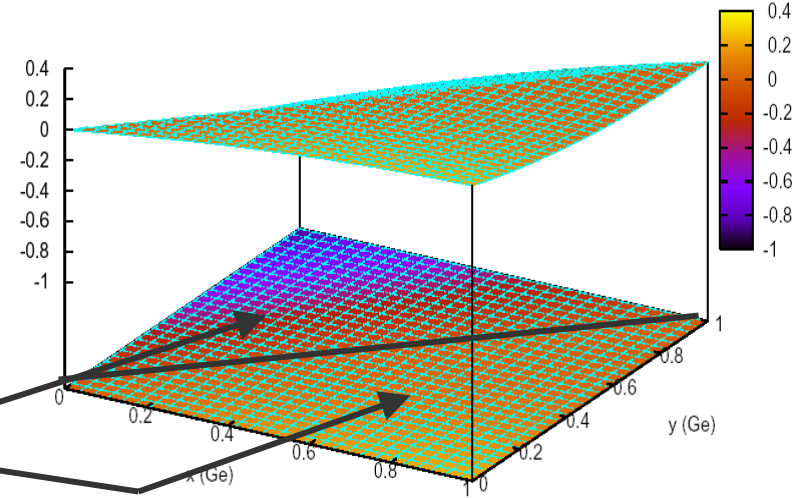
Strained $\text{Si}(1-x)\text{Ge}(x)$ /Unstrained $\text{Si}(1-y)\text{Ge}(y)$

Valence Band Split (eV)



Tensile strain

Cond. Band Discont. (eV)



Compressive strain

Implemented in Crosslight material macro library

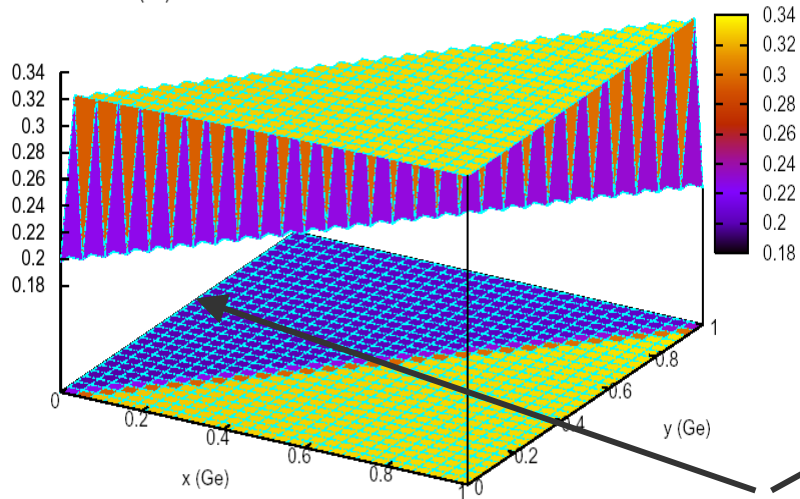
Strained $\text{Si}(1-x)\text{Ge}(x)$ on relaxed $\text{Si}(1-y)\text{Ge}(y)$ (Rieger&Vogl, Phys. Rev B48, 14276)

Parameterization of Effective Masses.

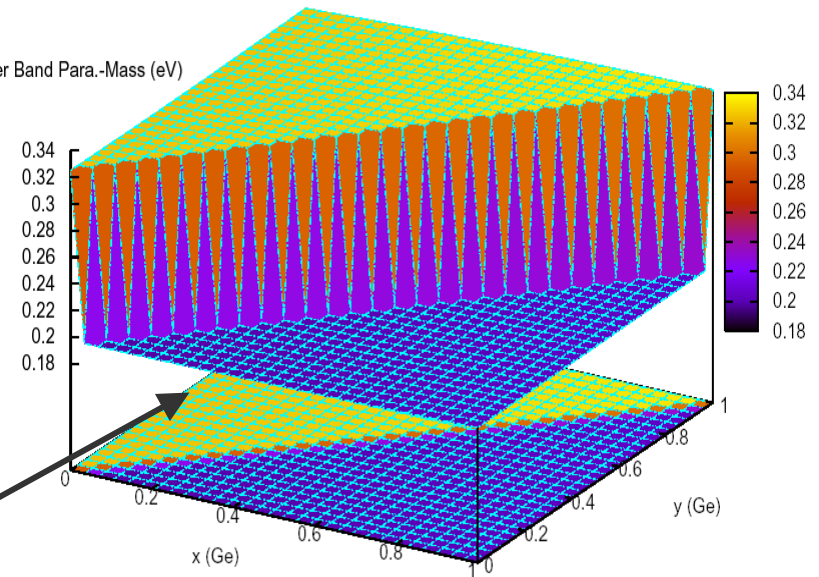
Strained Si(1-x)Ge(x)/Unstrained Si(1-y)Ge(y)

Strained Si(1-x)Ge(x)/Unstrained Si(1-y)Ge(y)

Lower Band Para.-Mass (eV)



Higher Band Para.-Mass (eV)



Wish to be here

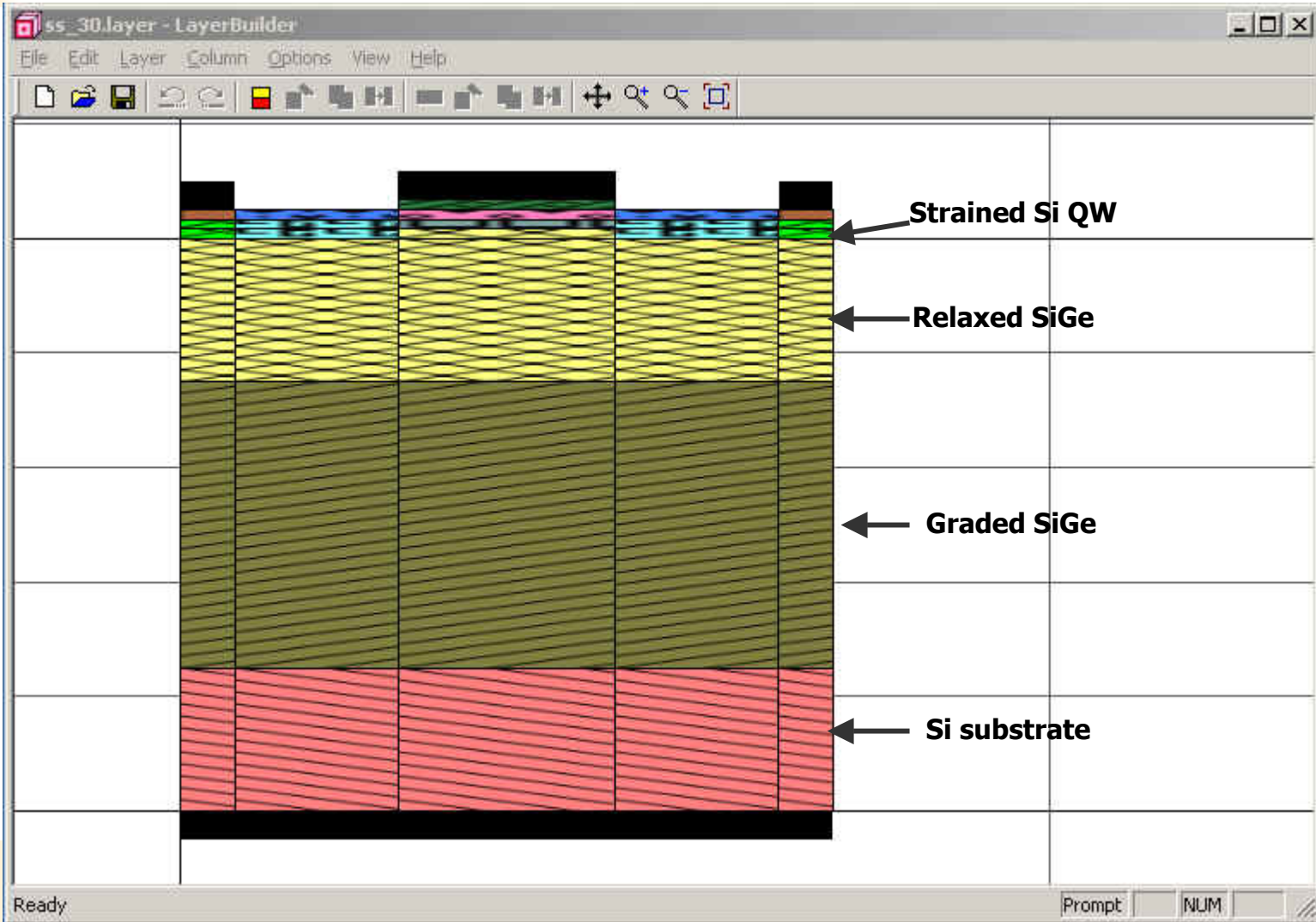
Implemented in Crosslight material macro library

Strained Si(1-x)Ge(x) on relaxed Si(1-y)Ge(y) (Rieger&Vogl, Phys. Rev B48, 14276)

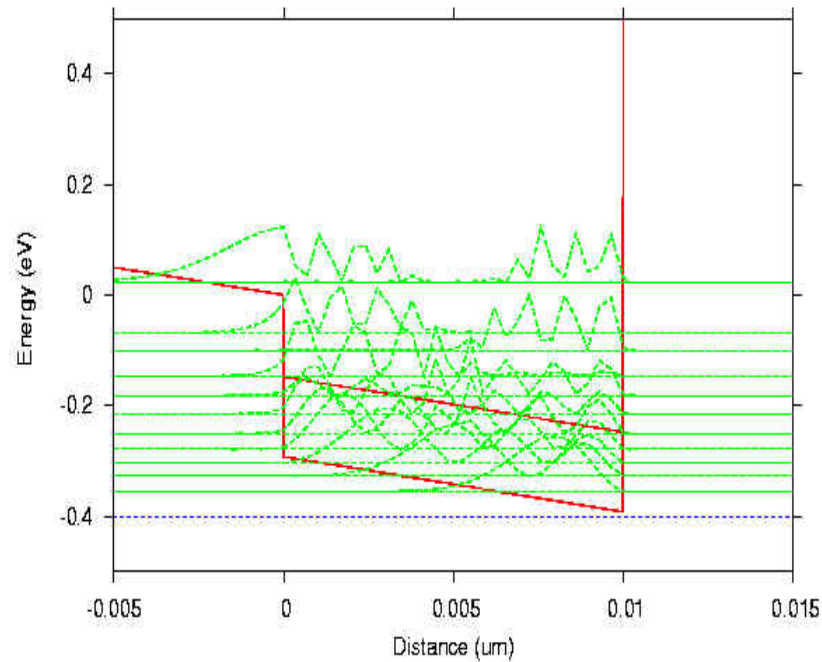
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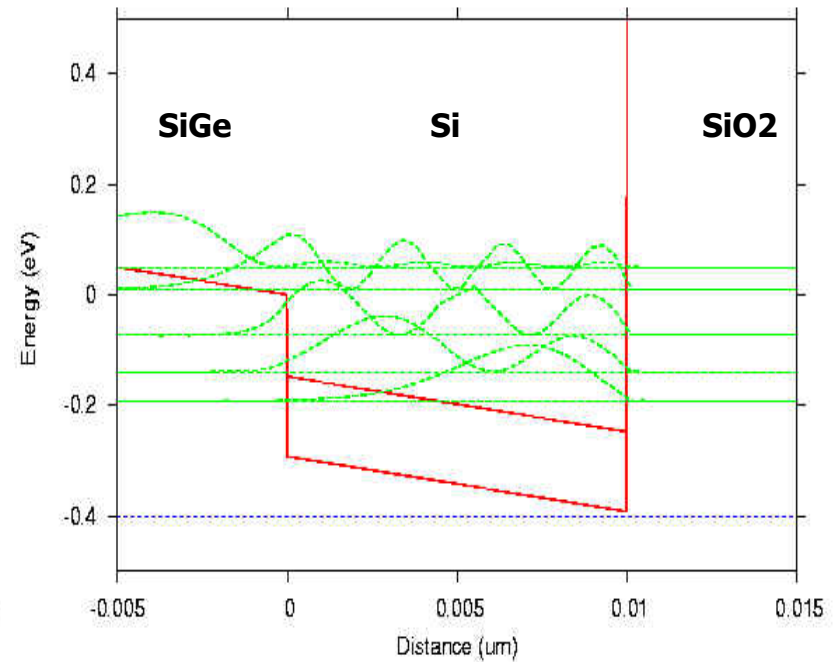
A simple 2D strained MOSFET structure



Quantized Electron States in Si/SiGe

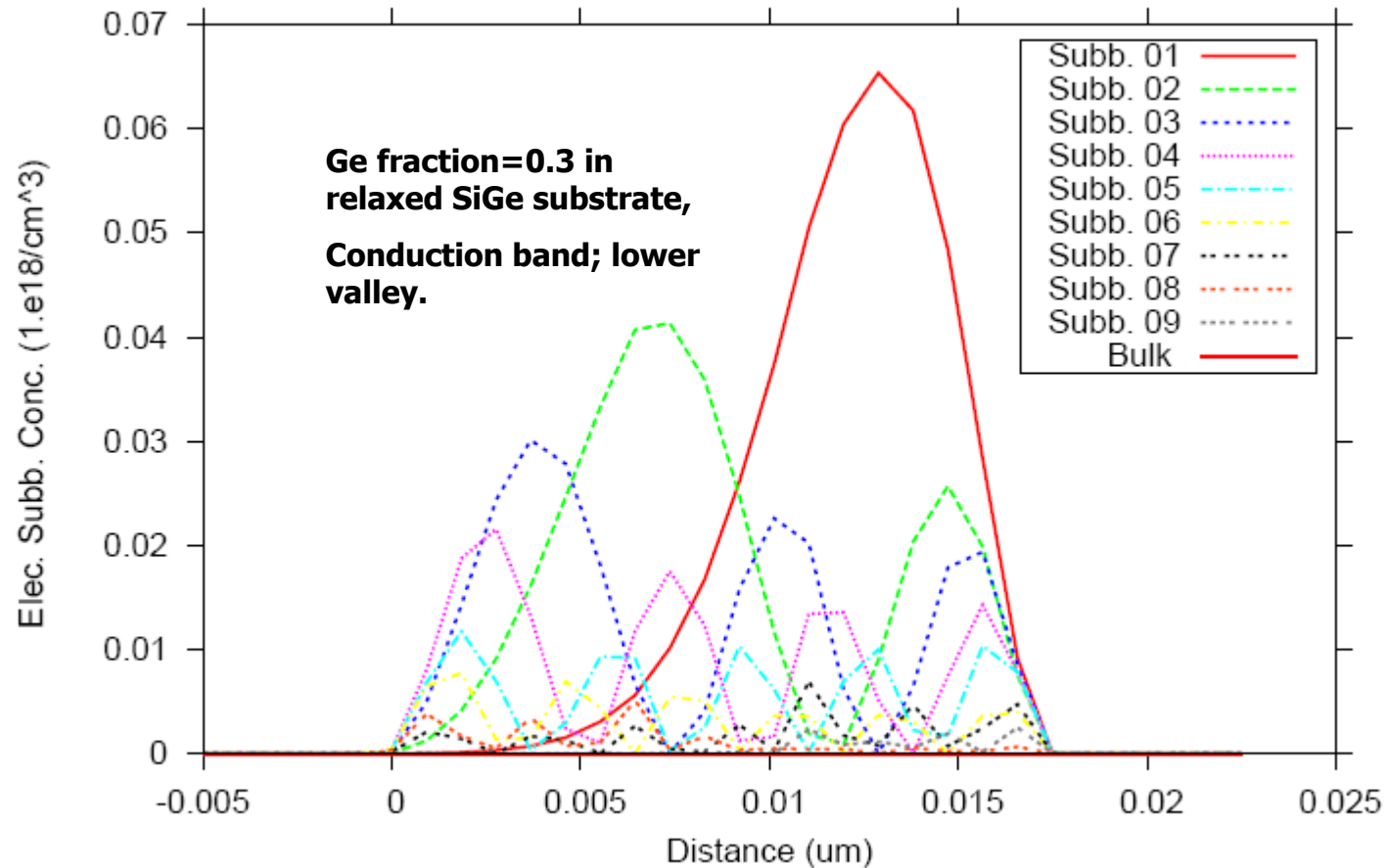


**Lower valley: smaller parallel mass
but larger perpendicular mass.**



**Higher valley: larger parallel mass
but smaller perpendicular mass.**

Carrier densities in Si/SiGe QW



Carrier density in each subband for different band valleys → weighted average of physical quantities such as mass dependent mobility

Simulated Mobility Enhancement for Si/SiGe MOS (biaxial tensile strain)

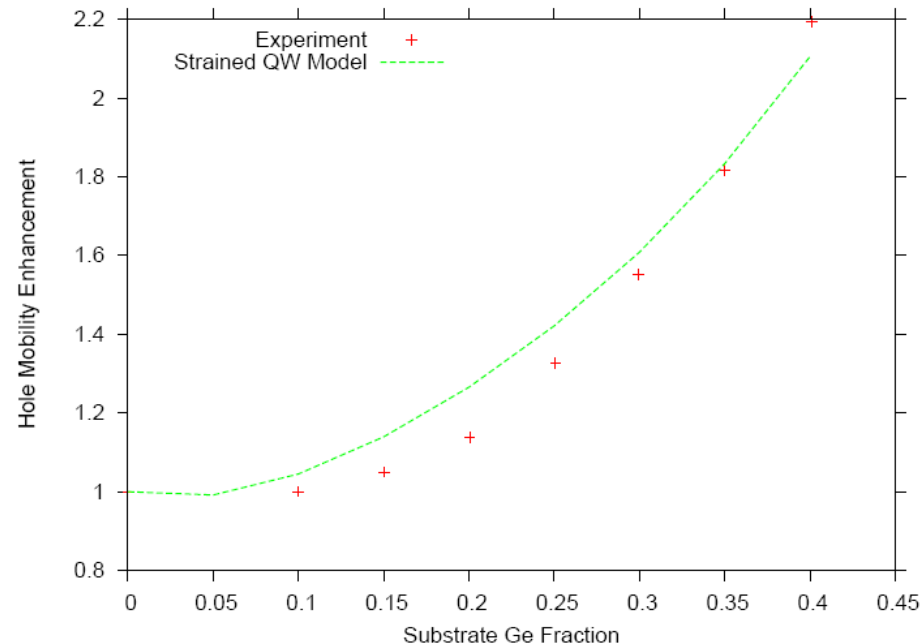
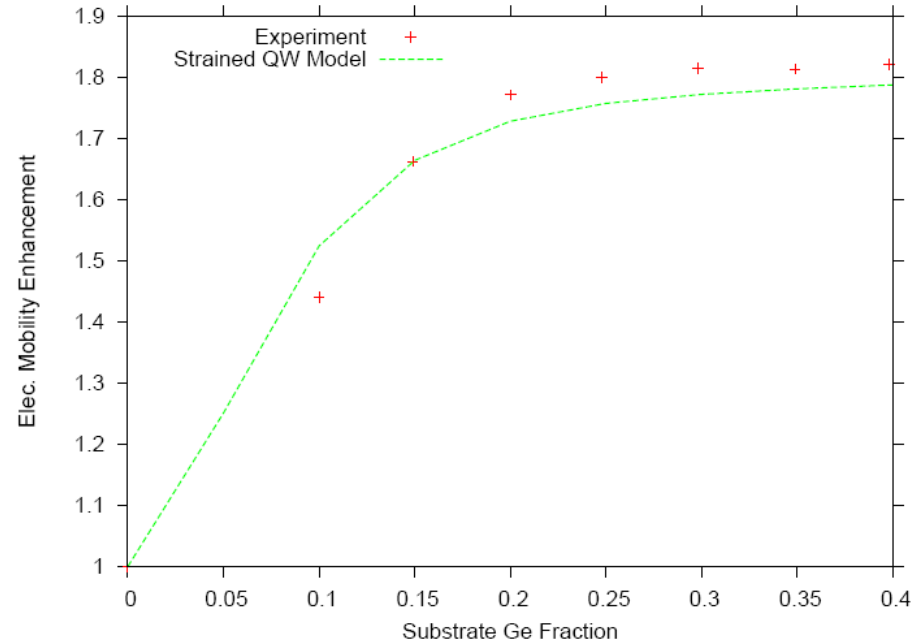
Effective mass change + valley splitting

→ mobility in each confined quantum state.

Quantum subband population weighted average

→ Channel mobility enhancement

→ Id-Vd prediction

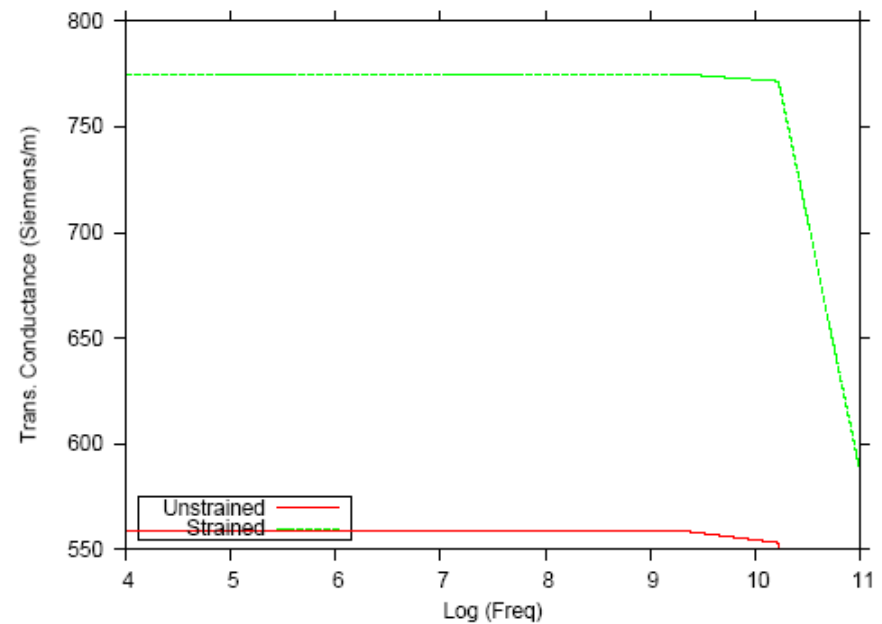
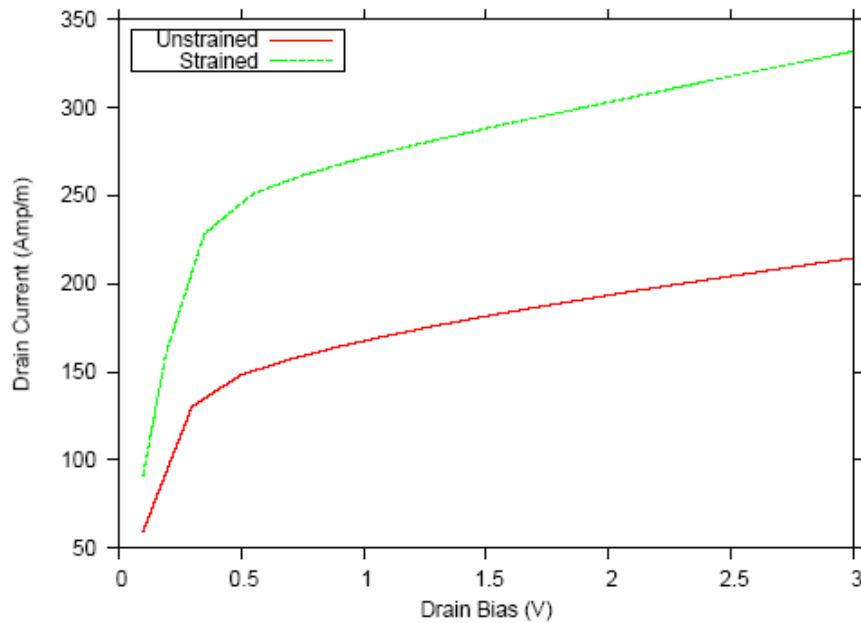


Experimental data taken from [1] and [2]:

[1] M. T. Currie, et.al, J. Vac. Sci. Technol. B 19(6), Nov/Dec. 2001, pp. 2268-2279

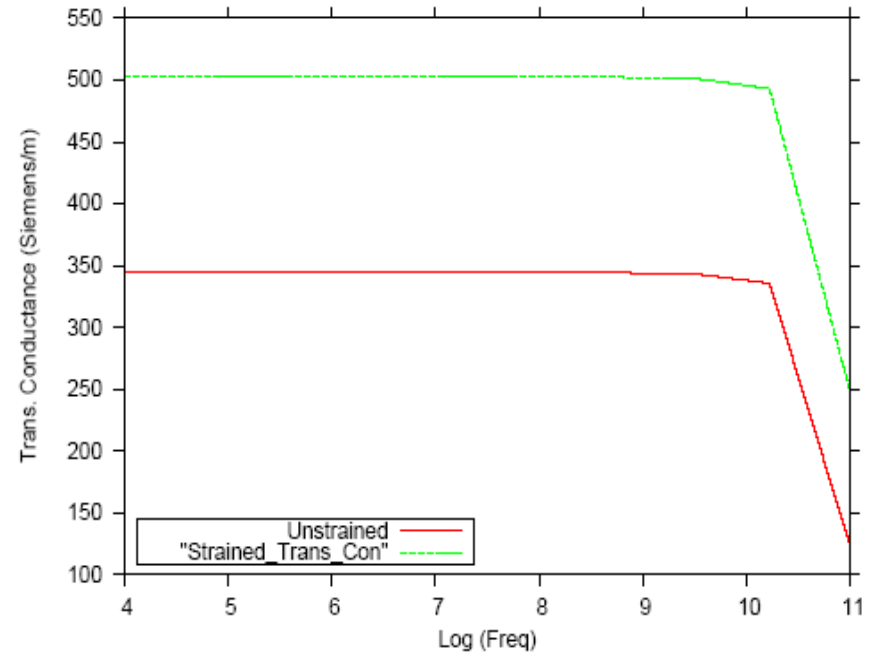
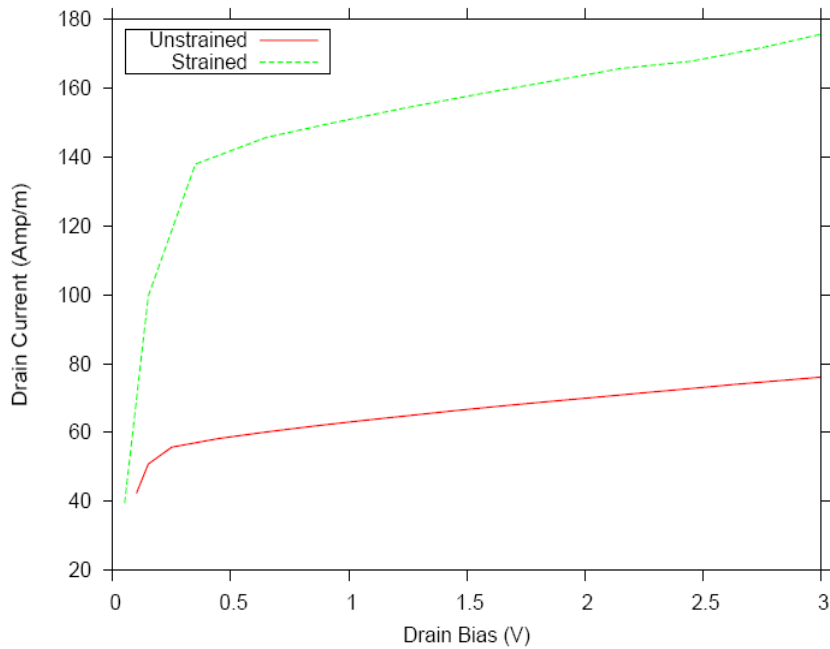
[2] M. Bulsara, Compound Semiconductor magazine, (September 2002)

Simulated drive current for a Si/SiGe (biaxial tensile) n-MOSFET based on strained QW model



Ge fraction =0.3 biaxial tensile channel=17.5 nm

Benefits for a Si/SiGe p-MOSFET based on Crosslight's QW model

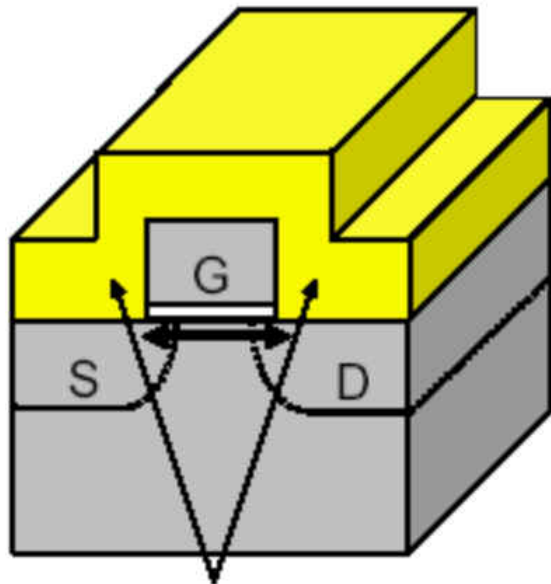


Ge fraction =0.3 biaxial tensile channel=17.5 nm

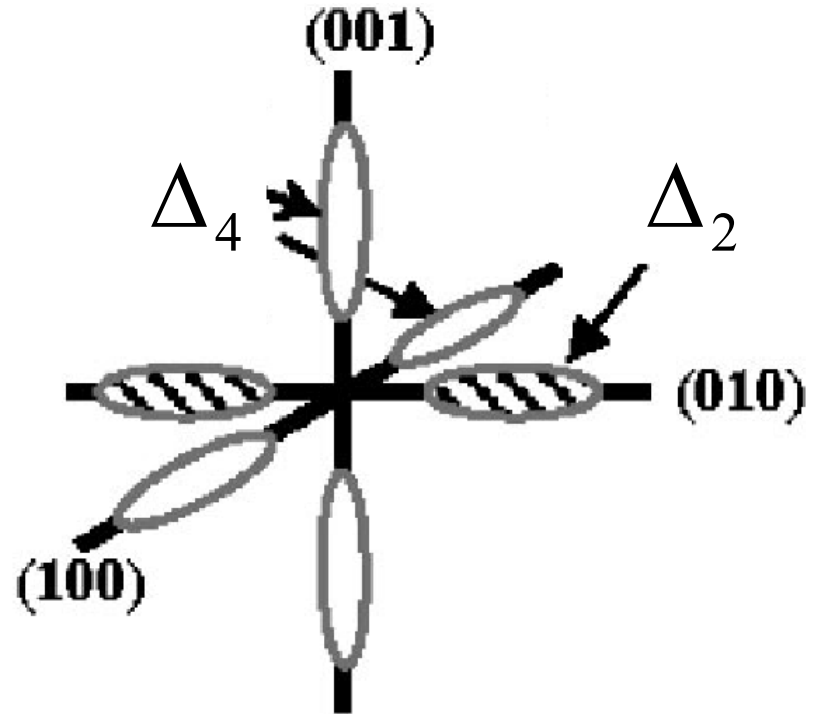
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Uniaxial Tensile Strained-Silicon [100] direction

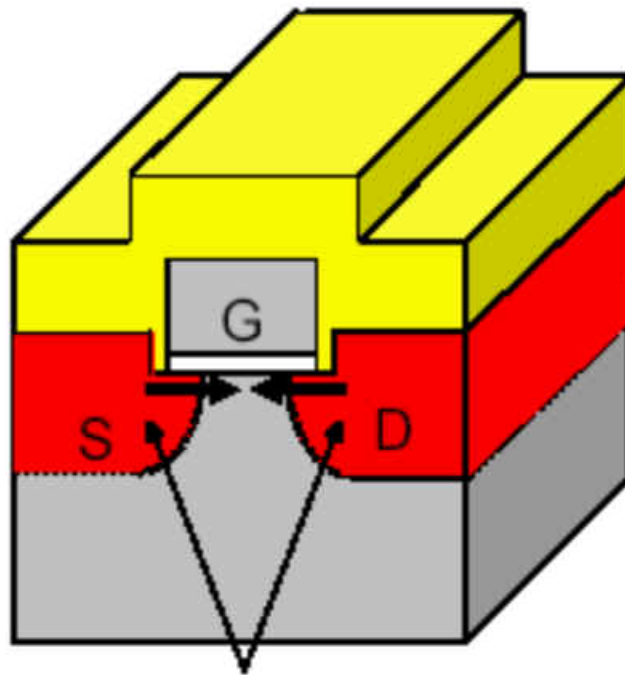


Tensile Si_3N_4 Cap

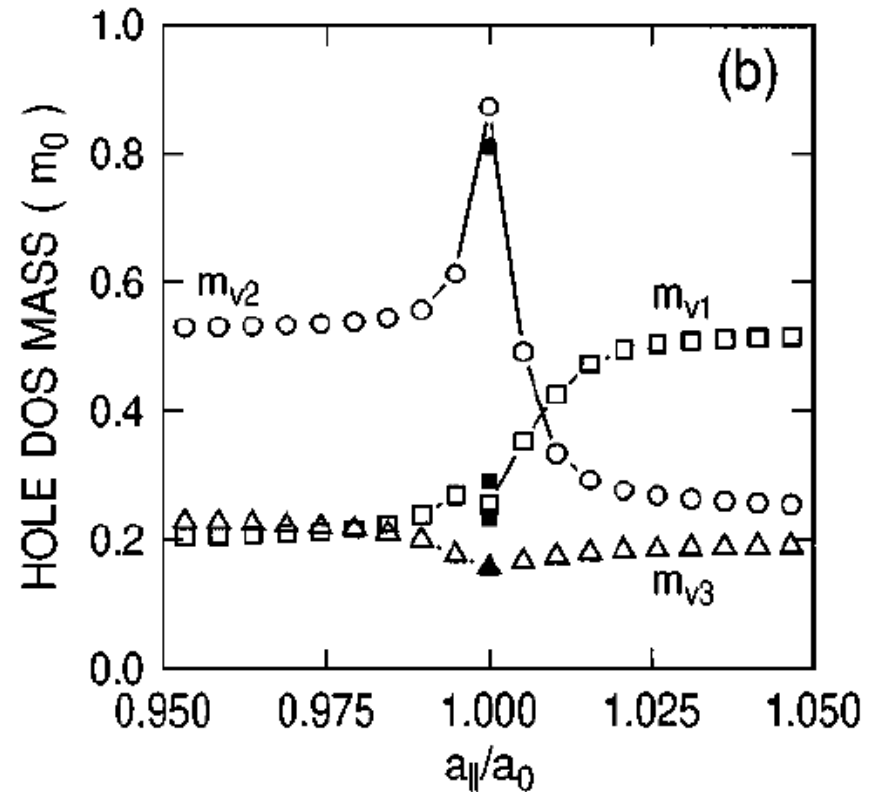


Delta4 has lower energy
 → transport/parallel mass = m_t
 → Good for mobility enhancement.

Uniaxial Compressive Strained-Silicon (PMOS)



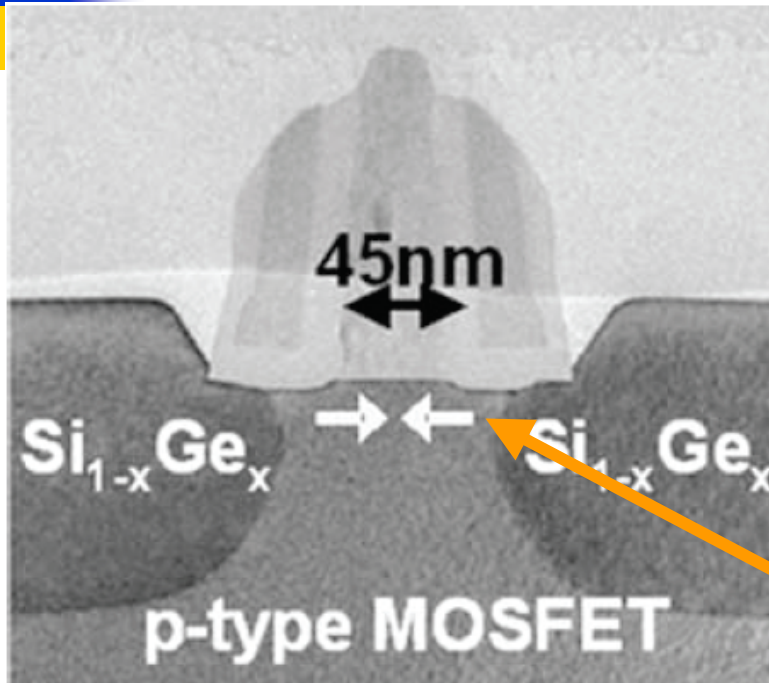
Selective SiGe S-D



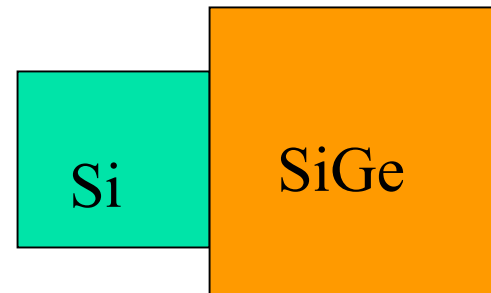
Ref: M.V. Fischetti and S.E. Laux,
J. Appl. Phys., vol. 80, pp. 2234-
2252, 1996.

Remark: Tensile biaxial strain splits HH/LH and quickly reduces the Heavy hole mass.

Conversion of parameters from biaxial to uniaxial



Lattice unit cell
before SiGe growth:



After SiGe growth:



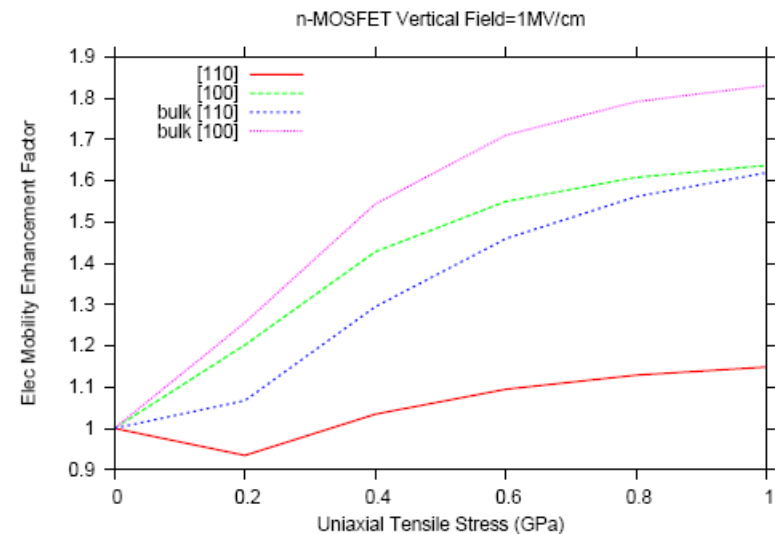
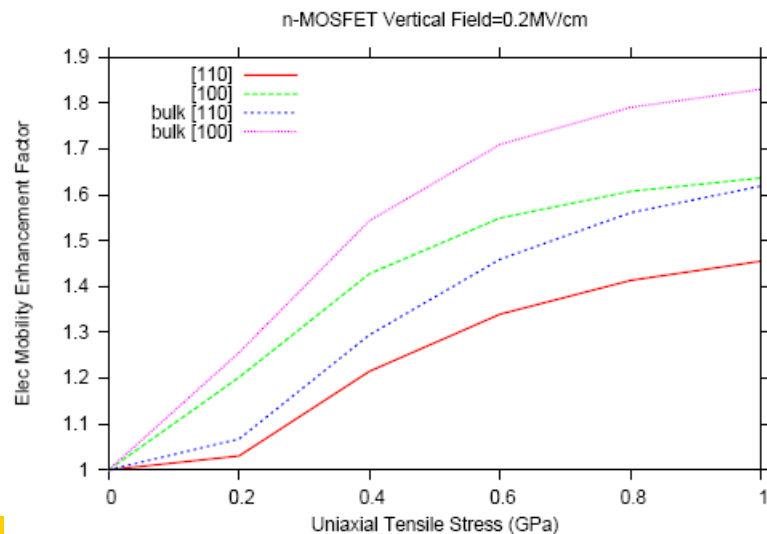
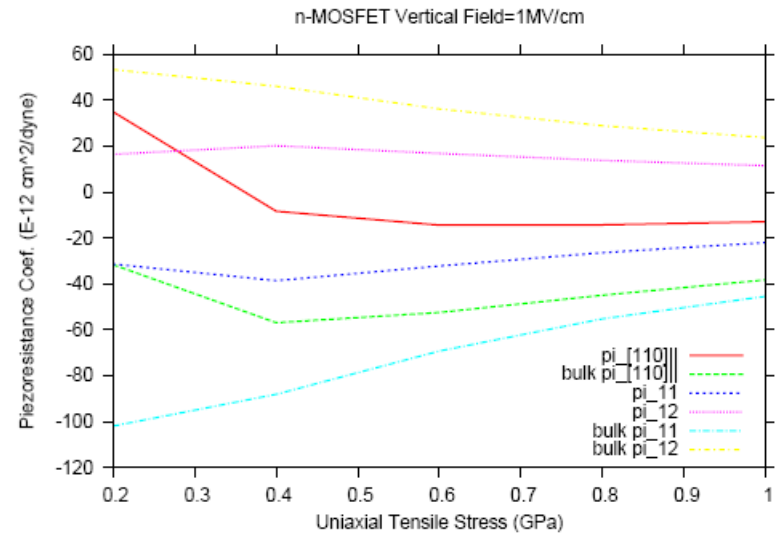
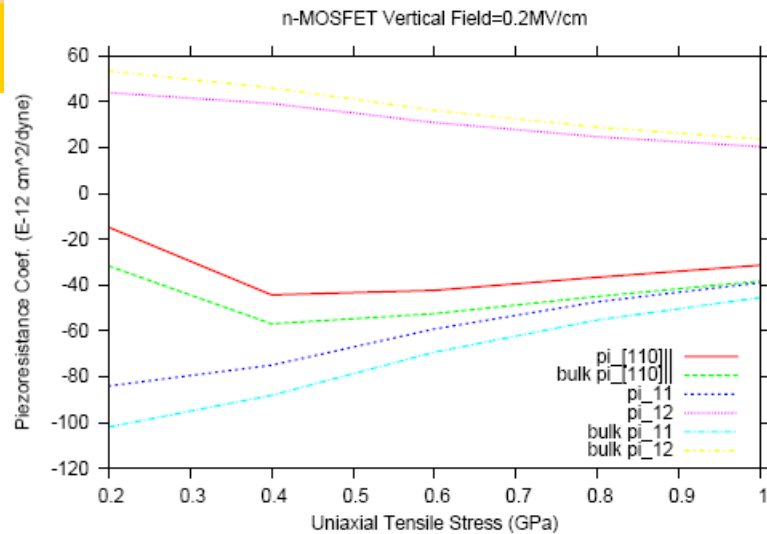
S_{xx}

Direction of force

Assuming perfectly matched lattice constant in planes parallel to Si/SiGe interface + given thicknesses in xx direction

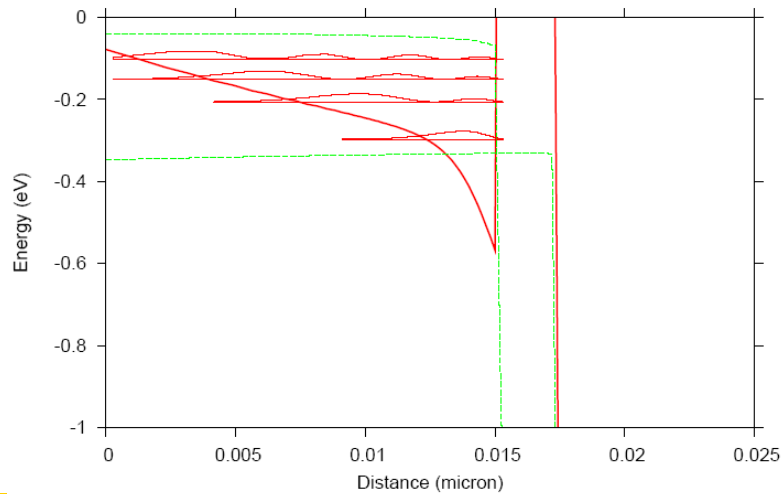
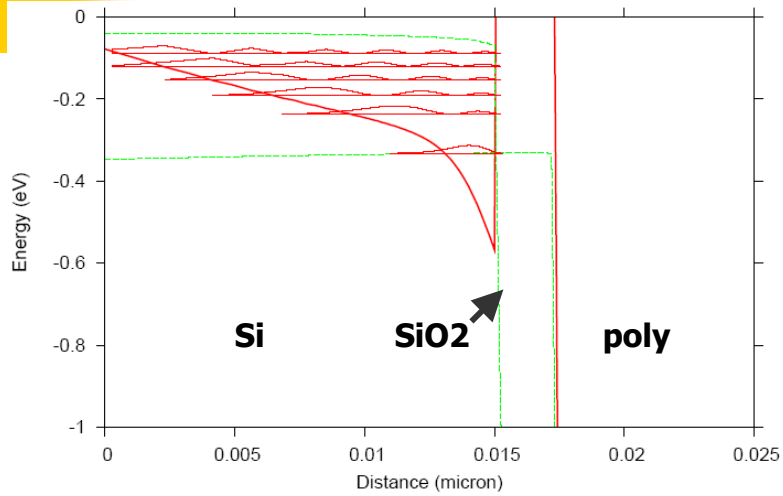
→ Convert strain from biaxial to uniaxial so that all calibrated data from Si/SiGe data base can be used for uniaxial strained silicon

Simulated Electron Mobility Enhancement

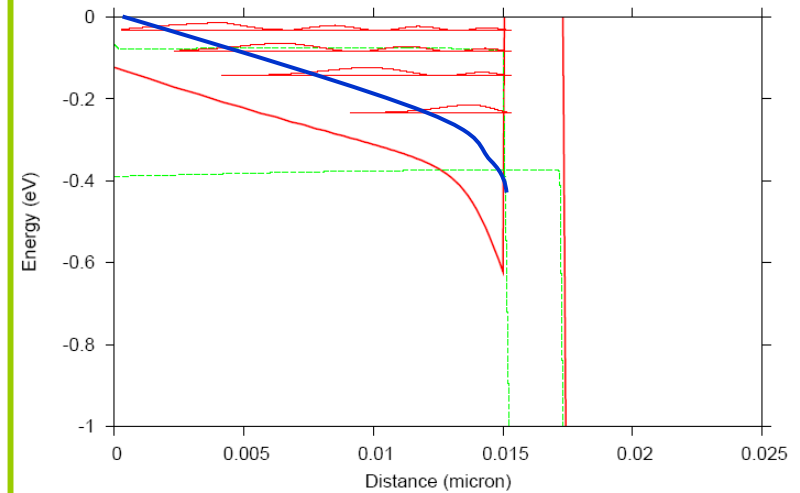
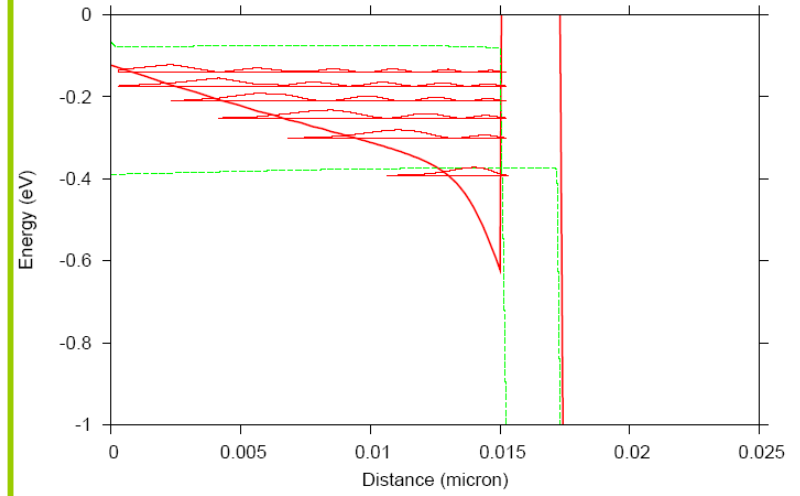


→ Effect of quantization is substantial due to large valley splitting

Quantized states of conduction band valleys



Stress=0



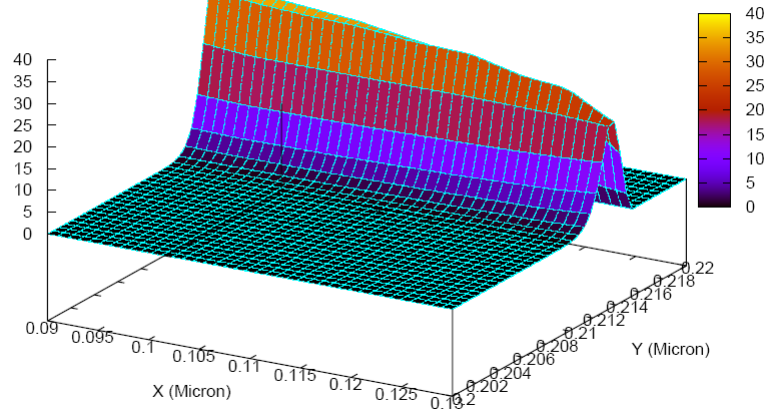
Uniaxial tensile stress=1 GPa

N-MOSFET Gate length=80 nm, $V_g=2$ V, $V_d=3$ V

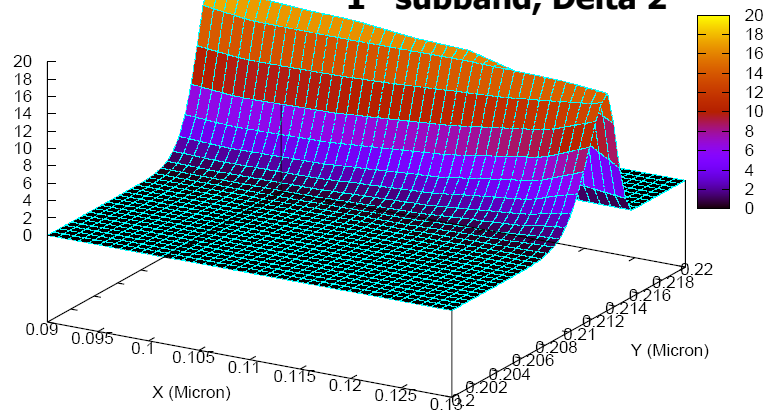
2D profile of quantized electron states under the gate

Elec_Conc (E18/cm³)

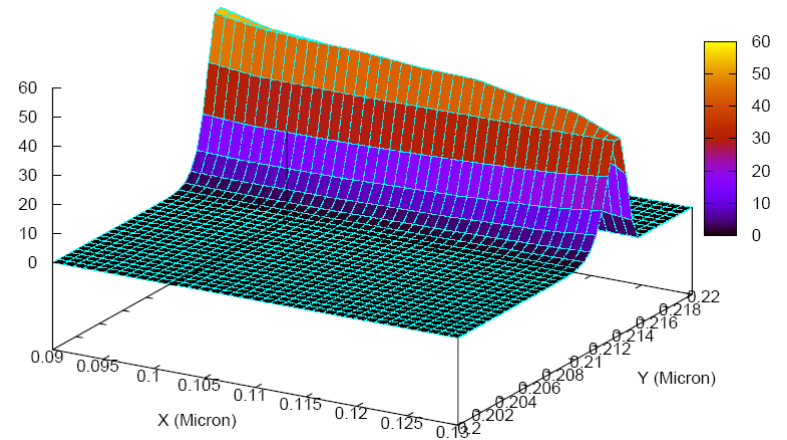
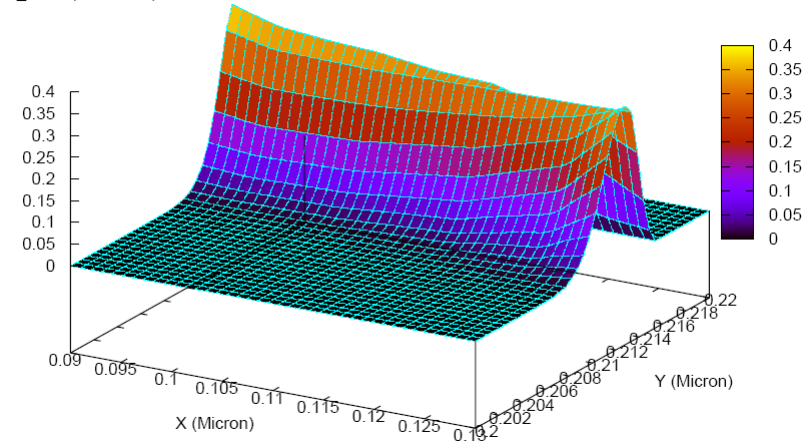
1st subband, Delta 4 valley

Elec_Conc (E18/cm³)

1st subband, Delta 2



Stress=0

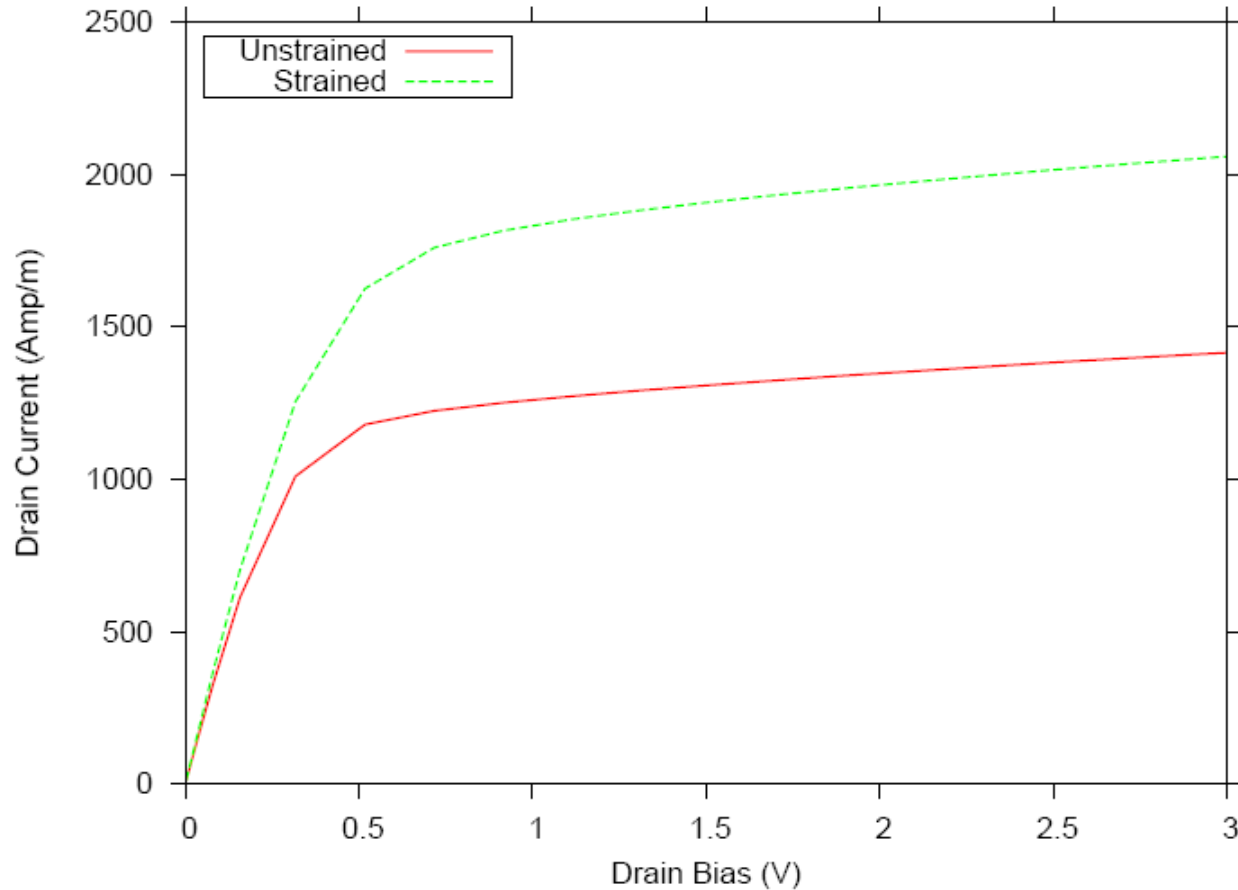
Elec_Conc (E18/cm³)Elec_Conc (E18/cm³)

Uniaxial tensile stress=1 GPa

Gate length=80 nm, $V_g=2$ V, $V_d=3$ V

Remark: tensile stress strongly affects subband population

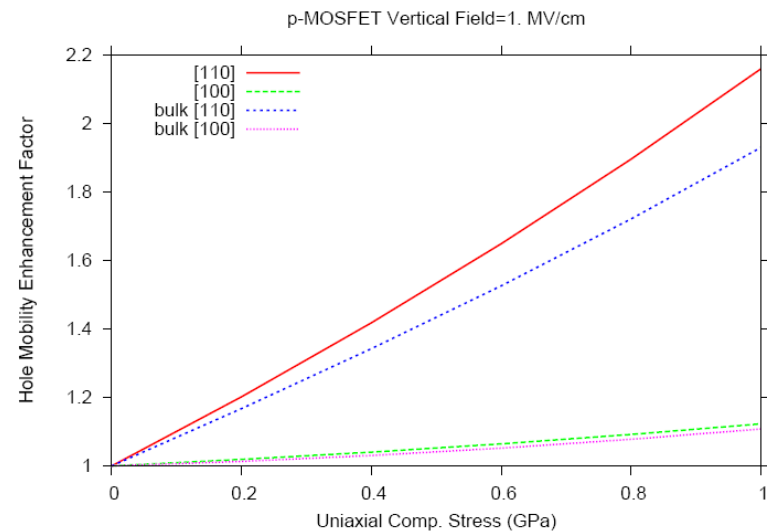
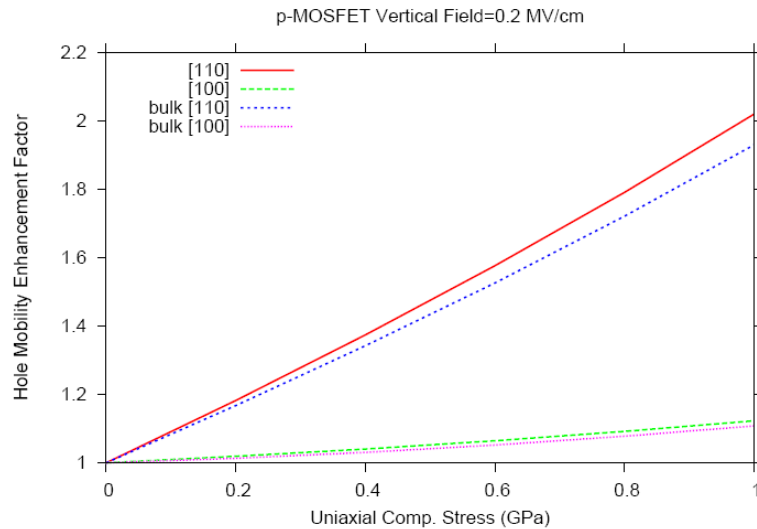
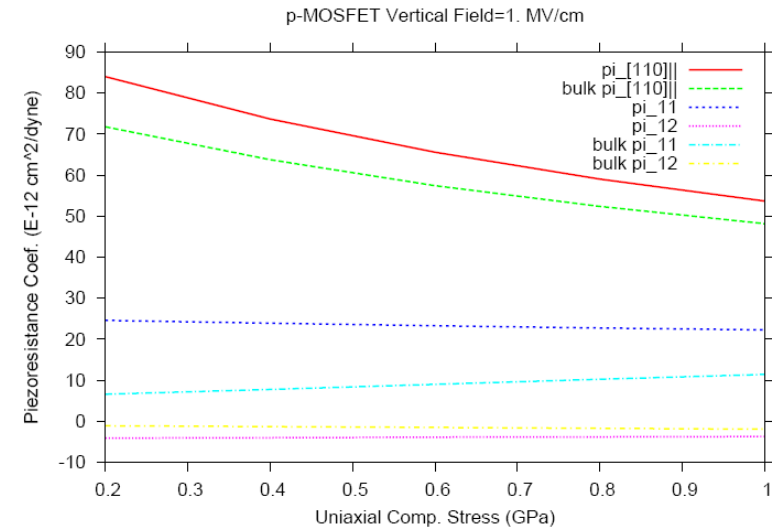
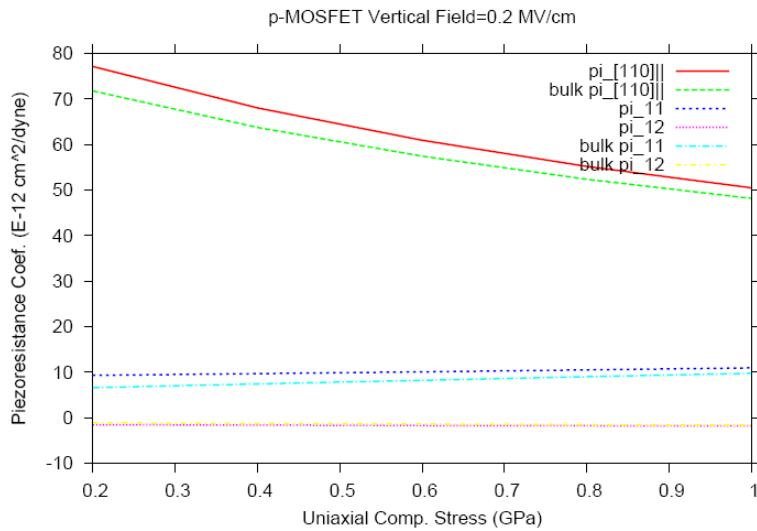
Benefits for typical Ux-S-Si n-MOSFET based on simulation



Gate length=80 nm, Uniaxial tensile stress=1GPa

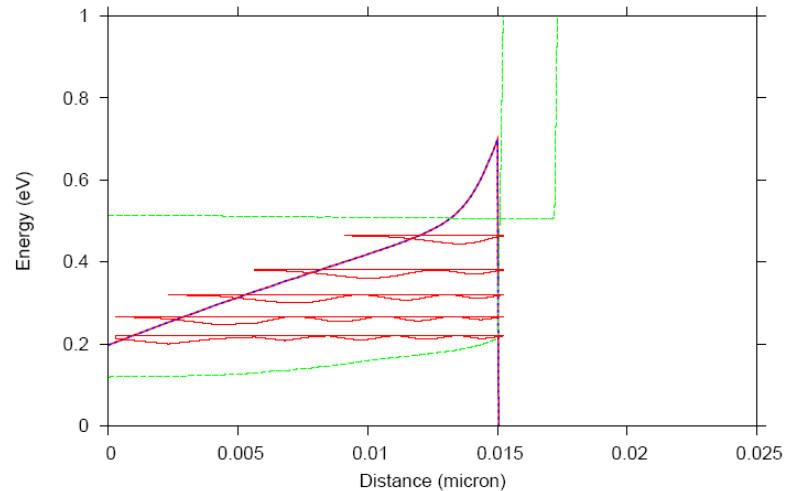
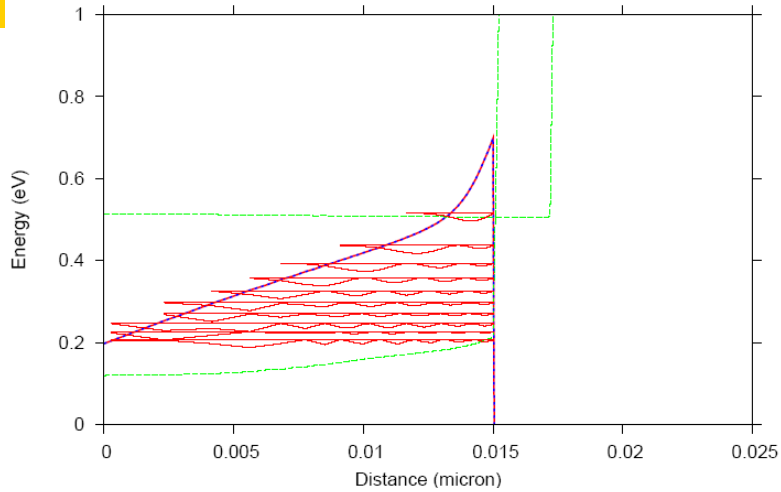
Saturation velocity enhancement=80 % of mobility enhancement

Simulated Hole Mobility Enhancement

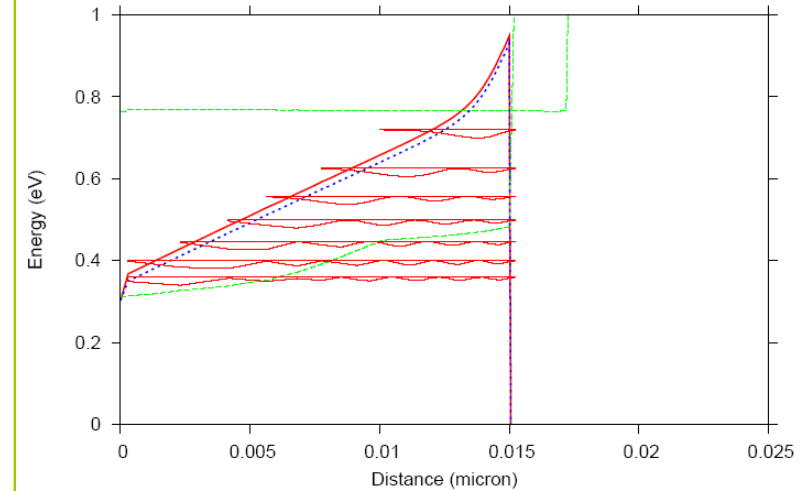
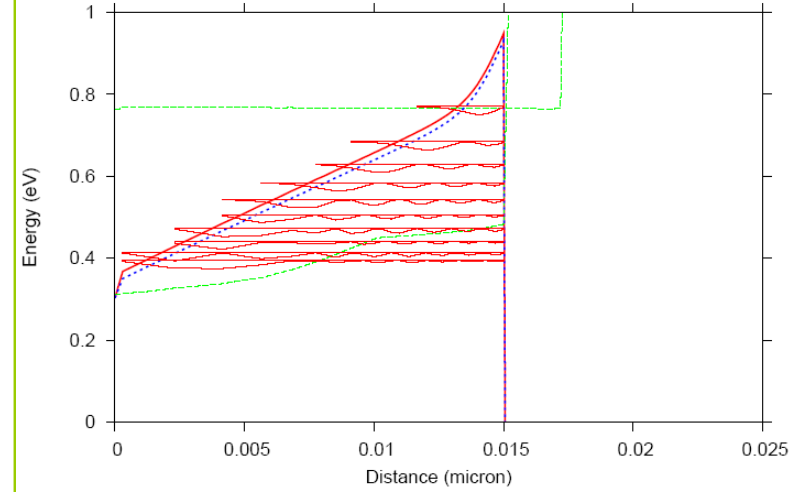


➔ Effect of quantization is less pronounced due to heavier mass and smaller valley splitting as compared with its electron counterpart.

Quantized states of valence band valleys



Stress=0



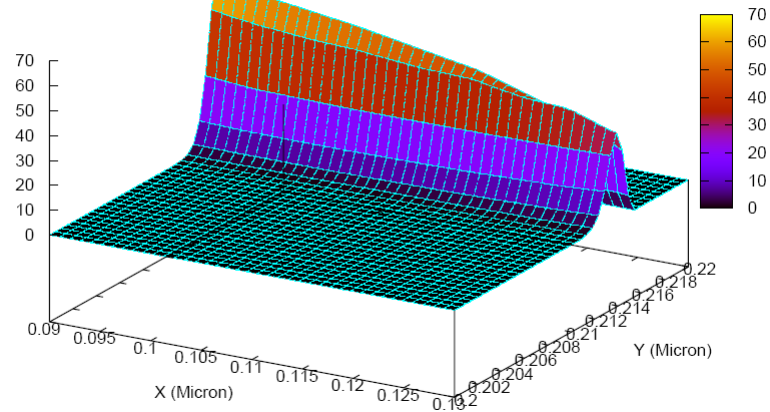
Uniaxial compressive stress=1 GPa

N-MOSFET Gate length=80 nm, $V_g=-2$ V, $V_d=-3$ V; Notice the shift in potential

2D profile of quantized hole states under the gate

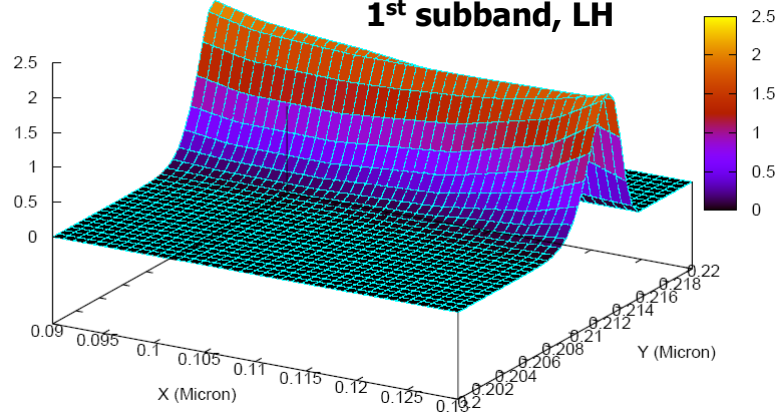
Hole_Conc (E18/cm³)

1st subband, HH valley



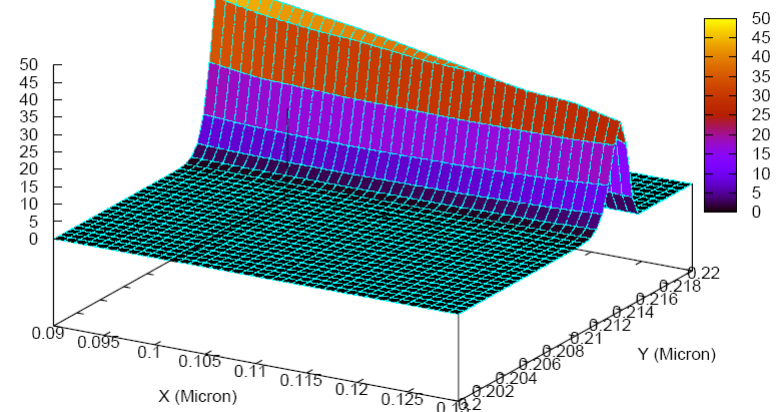
Hole_Conc (E18/cm³)

1st subband, LH

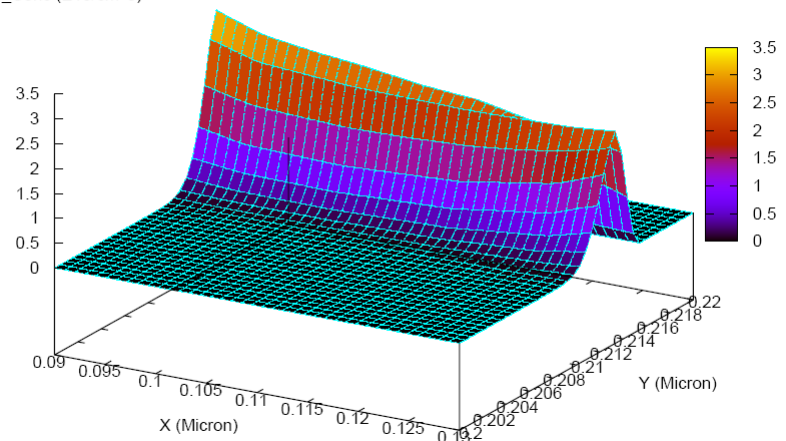


Stress=0

Hole_Conc (E18/cm³)



Hole_Conc (E18/cm³)

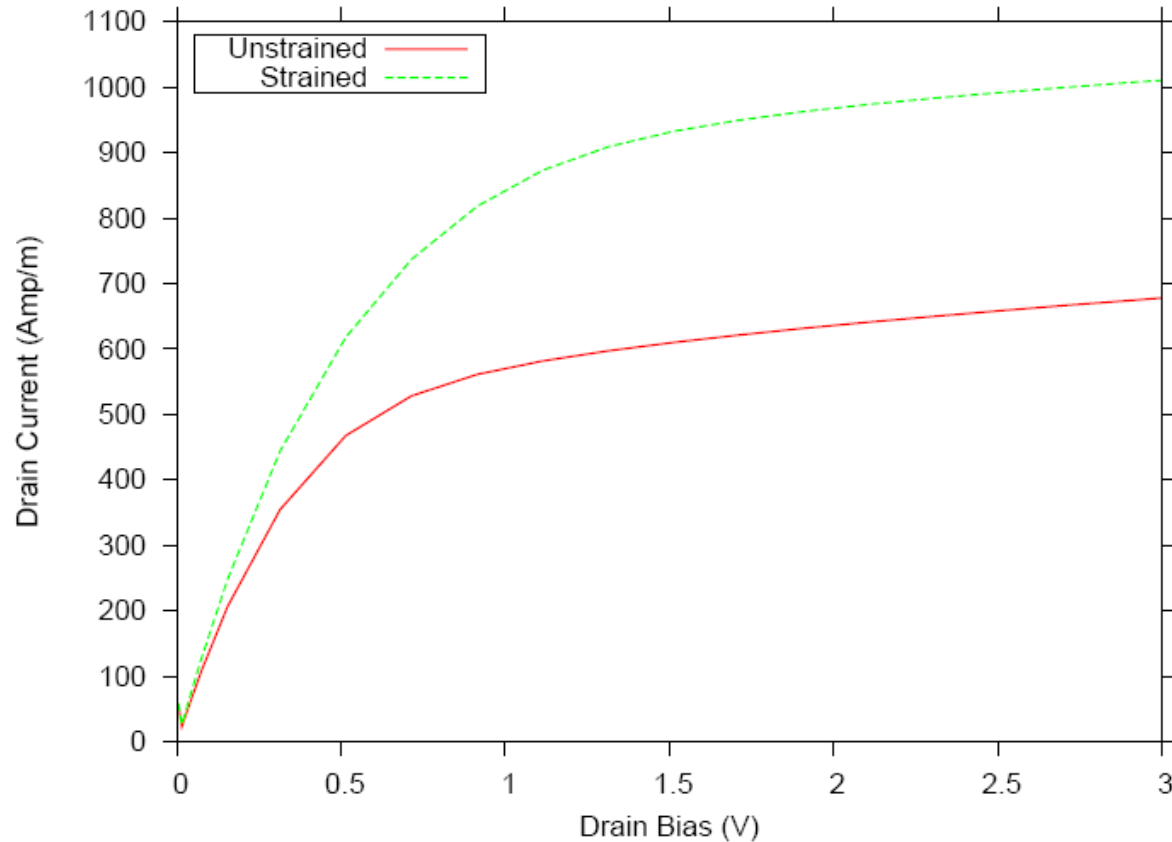


Uniaxial compressive stress [110]=1 GPa

Gate length=80 nm, $V_g=-2$ V, $V_d=-3$ V

Remark: stress affects subband population

Benefits for typical Ux-S-Si p-MOSFET [110] based on simulation



Gate length=80nm, Uniaxial compressive stress=1 Gpa

Saturation velocity enhancement=50 % of mobility enhancement

Conclusions

- **Crosslight's semi-classical quantum subband valley-averaged mobility model takes into account mass dependence, valley splitting and anisotropy.**
- **Enables self-consistent solution of drift-diffusion equations with quantum corrections using subband averaged density of states and mobility.**
- **Maybe used as TCAD to predict and optimize strained silicon MOSFET in various stress and crystal orientation.**